

ALTERNATIVES TO THE POPULATION PYRAMID FOR MAPPING  
AGE-SEX CHARACTERISTICS OF METROPOLITAN CENSUS TRACTS

Richard Lycan  
Center for Population Research and Census  
Portland State University, Portland, Ore. 97207

I. Introduction

Data on the age and sex of residents are extensively used in the planning of health care and other social services programs. This information must be available for small geographic areas, such as metropolitan census tracts, when planning facility locations or designing service delivery systems. Often it is desirable to utilize maps showing age-sex characteristics of tracts, either as a tool to help the planner visualize possibilities or to communicate alternatives to interested groups. Two types of maps are typically utilized to display such information: (1) choropleth maps for individual age-sex groups (eg: males 65 years or older) or (2) multiple population pyramids superimposed upon a base map. The choropleth map suffers by requiring as many maps as age-sex groups, making intergroup comparisons difficult. The use of pyramids permits a single map, but is visually so complex that comprehension of spatial patterns is difficult.

This paper describes and graphically displays several alternative approaches for mapping age-sex characteristics of metropolitan census tracts. These alternatives are based in part on a factor analysis that reduces the numbers of categories to be mapped from approximately 30 age-sex groups to two to four derivative components and permits the use of simpler mapping symbology than the age-sex pyramid. The alternative displays include: (1) a typology of pyramids for use in the legend of age-sex pyramid maps which facilitates

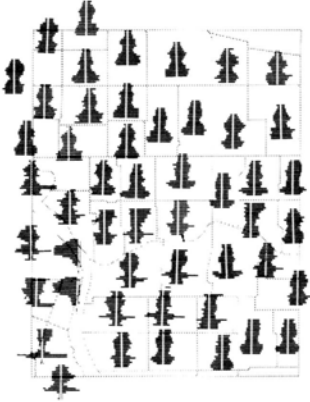
reading this complex type of map, (2) a process color map, which can be computer produced, showing areas of particular types of age-sex characteristics, and (3) a polar coordinate type symbol which may better allow the viewer's eye to detect qualitative differences in age-sex characteristics of metropolitan area tracts. Analyses carried out for two cities (Madison, Wis. and Portland, Ore.) suggest that these techniques can be generalized.

## II. Conventional Displays for Age-Sex Data

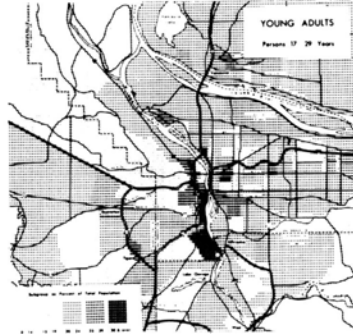
The most common form for the graphic display of age-sex information is the population pyramid, illustrated here for a major part of a metropolitan area (Figure 1). Population experts can look at the profiles of such pyramids and recognize the effects of the "great depression", the "post World War II baby boom" and even events unique to the local area. Two pyramids can be compared by superimposing them or simply viewing them adjacent to each other. However, when a large number of pyramids are simultaneously displayed, even a trained demographer has difficulty making sense of the geographic patterns. There are two main reasons for this confusion: (1) When many pyramids must be presented in a small space, as on a book page sized map, the legibility of the labeling of the age groups cannot be preserved. The reader can easily identify the youngest and oldest age groups at the upper and lower extremes of the diagram, but must count lines or make rough intuitive judgments of the vertical position for the intermediate age groups. These processes are slow, frustrating and error prone. (2) When pyramids are used to show census tract age-sex characteristics, tracts are usually chosen which highlight the phenomena being illustrated. The population pyramids for skid row tracts, tracts including college dormitories, or tracts of newly built suburban housing are easy to recognize. However, most metropolitan census tracts are heterogeneous due to aggregation of two or more dissimilar areas or to changes occurring over time, such as the gradual resettlement of older neighborhoods by younger families. Where such heterogeneity exists, the resultant pyramids can be difficult to interpret.

Spatial patterns can be seen better in choropleth maps of individual age groups (Figure 2). Where the age group under consideration is clearly defined, such as

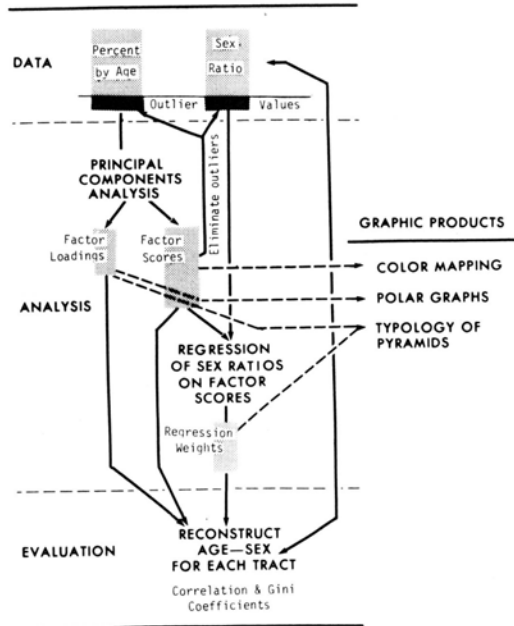
**FIG. 1  
POPULATION PYRAMIDS**



**FIG. 2  
CHOROPLETH MAP  
FOR AGE GROUPS**



**FIG. 3 FLOW CHART FOR MODEL**



by a law pertaining to persons 65 and over, such a map may adequately depict the geographic distribution. However if the reader needs to comprehend information about and relations between several age groups the limitations of the human eye and mind make it difficult for the reader to utilize the information displayed simultaneously on maps of several age groups. There also can be a problem in the aggregation of various ages into a single age group. For example, a map of the five year age group 15 to 19 can be somewhat confusing because it includes both persons living at home with parents and those who have established separate households.

### III. The Model Employed for Data Reduction

Age-sex data for census tracts for Madison, Wisconsin and Portland, Oregon were Factor analyzed in order to reduce the complexity of the data and thus allow the use of simpler maps to display complex data. The model utilized is diagramed in Figure 3 and the results are graphically displayed in Figures 4 and 5. Interested persons may contact the author for a more detailed discussion of the methodology or a copy of the computer program used in the analysis.

The data analyzed is the same as that displayed on a population pyramid (Figure 1). Age composition and sex composition are analyzed separately (Figure 3) as "percent by age" and "sex ratio", the number of males per female. The percent by age data were transformed by means of a square root transformation to reduce skewness and a small number of outlier values, such as skid row and student dormitory areas, were eliminated.

The percent by age data were subjected to a principal components type of factor analysis in order to produce factor loading and score matrices. The eigenvalues (Figure 4) indicate that the first four and especially the first two factors account for most of the variation in age structure. The factor loading diagrams (Figure 5) are quite similar for the two cities. Those groups found near each other on the diagrams tend to be co-located in actual city space as well. The third and fourth factors are smaller and result mainly from a few concentrations of young adult populations, such as those clustered around college campuses.

Table 1. Example of Data for One Tract

Tract 1.00	Age Group									Total	
	00-04	05-09	10-14	15-17	18-24	25-34	35-44	45-54	55-59		60+
Males	143	141	158	91	228	226	155	167	66	107	1482
Females	115	161	136	83	195	219	170	178	55	142	1454
Persons	258	302	294	174	423	445	325	345	121	249	2936
% by age	.088	.103	.100	.059	.144	.152	.111	.118	.041	.085	-
$\sqrt{\%}$ by age	.296	.321	.316	.243	.380	.389	.333	.343	.203	.291	-
Sex ratio	1.24	0.87	1.16	1.10	1.17	1.03	0.91	0.94	1.20	0.75	-

FIG. 4 EIGENVALUES FOR PERCENT BY AGE DATA

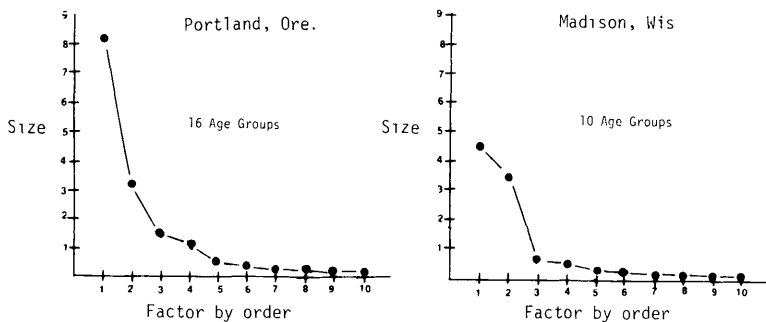
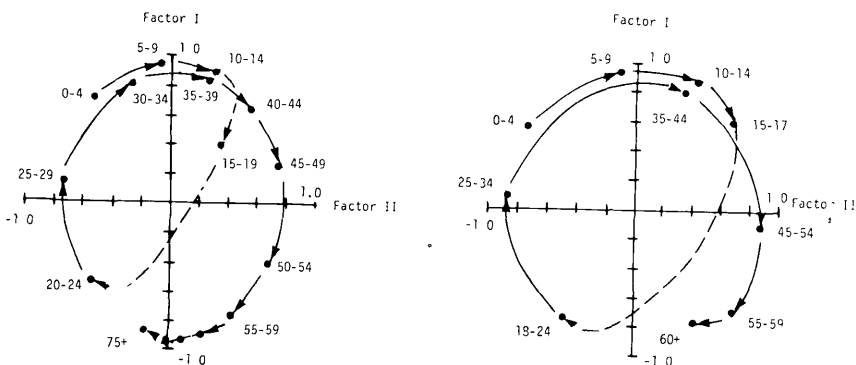


FIG. 5 FACTOR LOADINGS FOR PERCENT BY AGE DATA



So far the analysis has been concerned only with age distributions, not the varying proportions of males and females. A regression analysis was performed to find out whether it would be reasonable to view geographic sex ratio variations as largely explained by geographic age variations. The results suggest this to be true to some extent, but multiple correlations are not high.

As a check on the model the factor scores and loadings (for age factors I-IV) and regression weights for sex ratios were used to reconstruct the pyramids for each tract. The results were highly encouraging for the age data with about half the correlations between actual and estimated percent by age over .99. The results for sex ratios were not as good as shown by the correlation coefficients, but the errors as measured by Gini coefficients, were about equal in absolute terms to those for percent by age.

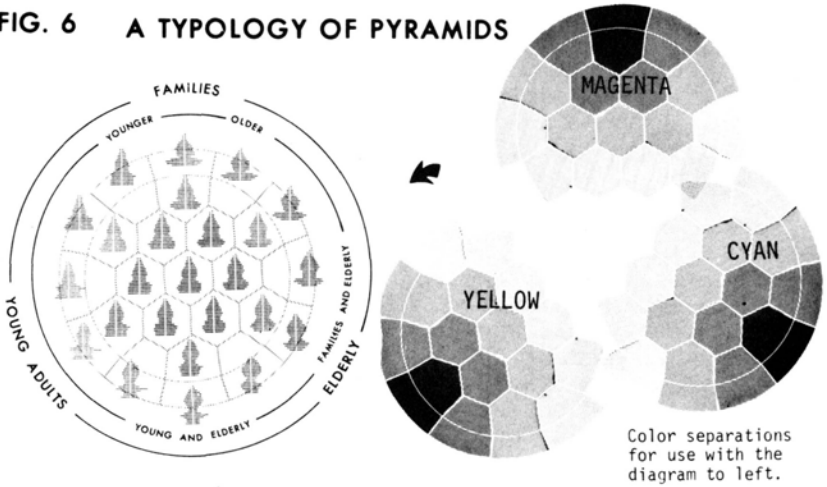
#### IV. Alternative Graphic Displays

The analysis described above allows a considerable reduction in complexity of the age-sex data. Several examples of maps stemming from this analysis are discussed below.

The first example is a legend intended to assist the reader in interpreting maps which are composed of "synthesized" population pyramids (Figure 6). This diagram provides the reader with a visual crutch which can help make sense of the sometimes bewildering variety of pyramids that appear on the map. These legend pyramids were constructed from the model's factor loadings and regression values.

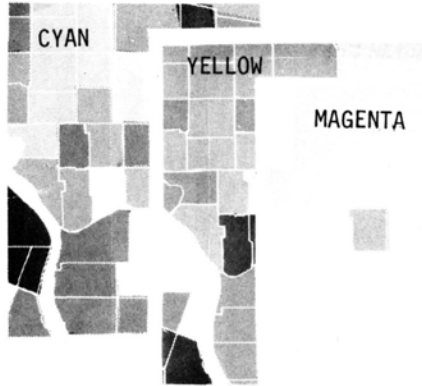
The second example is a map composed of color tones (Figure 7) which also are used in the map legend and are intended to allow the reader's eye to scan the map more rapidly. This color coding should aid the map reader in such tasks as (1) finding areas with certain types of population structures; (2) comparing areas; and (3) making general statements about regional trends and differences. Population pyramids (as in Fig. 1) can be printed over these tones, as could dots or other point or line symbols. The values for the color separations are factor scores for factors I and II from the age analysis, color standardized to key the mag-

**FIG. 6 A TYPOLOGY OF PYRAMIDS**

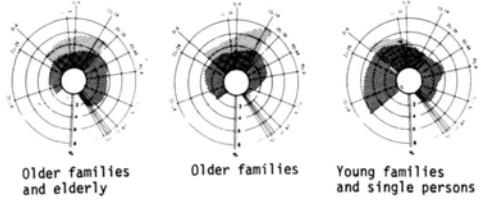


**FIG. 7 SEPARATIONS FOR COLOR MAP**

Age pyramids (Fig. 1) may be overprinted on three color age map.



**FIG. 8 POLAR DIAGRAM FOR AGE**



enta separation to the family age groups.

The third example is a polar coordinate graph which displays age structure, but not sex composition differences (Figure 8). The order of the age classes used in this display is the same as their location on age factors I and II. The logic of this placement is that groups which tend to be co-located in the city are placed in adjacent positions on the diagram. This diagram may be preferable to the population pyramid because (1) on a small symbol the reader can better identify individual age groups, (2) the qualitative distinctions between areas with differing age structures may be enhanced, and (3) spatially associated age cohorts are grouped together.

Whether these experimental diagrams are as effective as the traditional use of population pyramids on maps may be difficult to determine because the pyramid is so widely used and accepted. Nevertheless, the author is presently attempting to arrange for such testing. Efforts are also underway to carry out the data reduction analysis for additional cities in order to better evaluate the model's generality.

#### Sources Utilized

Board, Christopher. "Map Reading Tasks Appropriate in Experimental Studies in Cartographic Communication," The Canadian Cartographer, Vol. 15 (June 1978), pp.1-12

Guest, Avery. "Patterns of Family Location," Demography Vol. 9 (1972), pp. 159-172.

Robson, B.T. Urban Analysis. London: Cambridge University Press, 1969.

Schmid, Calvin F. and Stanton E. Schmid. Handbook of Graphic Presentation. New York: John Wiley & Sons, 1979

Shyrock, Henry S; Jacob Siegal et al. The Methods and Materials of Demography. Washington: U.S. Government Printing Office, 1971.

Wang; Peter C. C. (Ed.) Graphical Representation of Multivariate Data. New York: Academic Press, 1978.